

MATH 7 Accelerated: Week of April 20

- Go through the slides (notes) and work through the examples on a separate piece of paper.
- Do the given practice problems (again, on a separate piece of paper).
- Check your answers with the key given (last slide).
- If you have questions or would like feedback on your work, submit a photo/scan of it to google docs or return your work to the school Monday.
- If you do not have questions/need feedback, click on the "mark as complete" button on Google Docs.
- Check your school email/google calendar for online help sessions via Zoom.

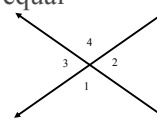
Day 1: Slides 2-5
Day 2: Slides 6-10
Day 3: Slide 11-15
Day 4: Slide 16-17
Answers on Slide 18

Day 1

L4: Vertical Angles & Linear Pairs

Vocabulary

Vertical Angles:
Nonadjacent angles formed by two intersecting lines. Vertical angles are equal in measure.



$\angle 1$ & $\angle 4$ are vertical angles.

Linear Pair: Two adjacent angles whose non-common sides are opposite rays. If two angles form a linear pair, they are supplementary angles.

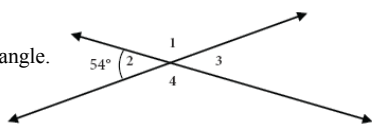
$\angle 1$ & $\angle 2$ are a linear pair.

Example 1

Find the measure of each missing angle.

a. $m\angle 3$

▶ Vertical angles are congruent.



$$m\angle 2 = m\angle 3$$

$$54^\circ = m\angle 3$$

b. $m\angle 1$

- ▶ $m\angle 1$ and $m\angle 2$ are a linear pair.
- ▶ Substitute known values.
- ▶ Subtract 54 from each side.

$$m\angle 1 + m\angle 2 = 180$$

$$m\angle 1 + 54 = 180$$

$$\begin{array}{r} -54 \\ -54 \\ \hline m\angle 1 = 126^\circ \end{array}$$

c. $m\angle 4$

▶ Vertical angles are congruent.

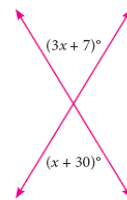
$$m\angle 1 = m\angle 4$$

$$126^\circ = m\angle 4$$

Example 2

Use the diagram to the right.

- Solve for x .
- Find the measure of each angle.



- Vertical angles have equal measures. Subtract x from each side.

$$3x + 7 = x + 30$$

$$\begin{array}{r} -x \\ -x \\ \hline 2x + 7 = 30 \\ -7 \\ -7 \\ \hline 2x = 23 \\ \div 2 \\ \div 2 \\ \hline x = 11.5 \end{array}$$

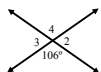
Subtract 7 from each side.

Divide by 2 on each side.

- Substitute the solution for x in each angle expression.
 $(3x + 7) = (3(11.5) + 7) = (34.5 + 7) = 41.5^\circ$
 $(x + 30) = (11.5 + 30) = 41.5^\circ$
 The measure of each angle is 41.5° .

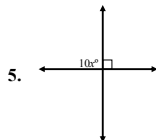
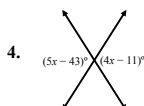
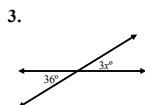
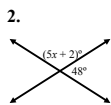
L4 Practice Problems:

- Determine the measure of each unknown angle using the diagram below.



- $m\angle 2 =$ ____
- $m\angle 3 =$ ____
- $m\angle 4 =$ ____

Identify each identified angle pair as vertical angles or a linear pair. Solve for x .



END DAY 1

Day 2

L5: Alternate Exterior and Interior Angles

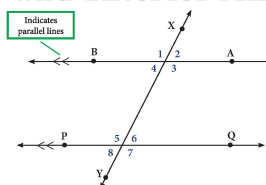
Vocabulary

Transversal: A line that intersects two or more lines in the same plane.

\leftrightarrow is a transversal

Alternate Exterior Angles: Two angles on the outside of two lines and on opposite sides of a transversal.

$\angle 1$ & $\angle 7$ are alternate exterior angles.



Alternate Interior Angles:

Two angles on the inside of two lines and on opposite sides of a transversal.

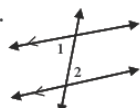
$\angle 4$ & $\angle 6$ are alternate interior angles.

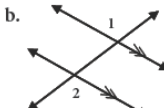
If two parallel lines are intersected by a transversal, then the alternate interior angles are congruent.

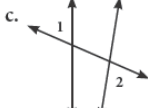
If two parallel lines are intersected by a transversal, then alternate exterior angles are congruent.

Example 1

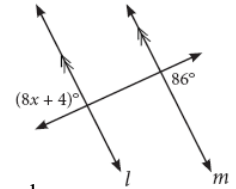
Name the angle relationship between $\angle 1$ and $\angle 2$.
Determine whether $\angle 1$ and $\angle 2$ are congruent.

a.  Alternate Interior Congruent – lines are parallel

b.  Alternate Exterior Not Congruent – lines are not parallel

c.  Alternate Exterior Congruent – lines are parallel

Example 2

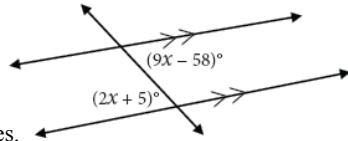


Identify the special angle pair relationship. Solve for x .

- The angles are alternate exterior angles.
- Lines l and m are parallel so the alternate exterior angles are congruent.

$$\begin{array}{r} 8x + 4 = 86 \\ -4 \quad -4 \\ \hline 8x = 82 \\ \div 8 \quad \div 8 \\ \hline x = 10.25 \end{array}$$

Example 3



Use the figure. Solve for x and find the measure of the angles.

- The lines are parallel so alternate interior angles are congruent.

$$\begin{array}{r} 9x - 58 = 2x + 5 \\ -2x \quad -2x \\ \hline 7x - 58 = 5 \\ +58 \quad +58 \\ \hline 7x = 63 \\ \div 7 \quad \div 7 \\ \hline x = 9 \end{array}$$

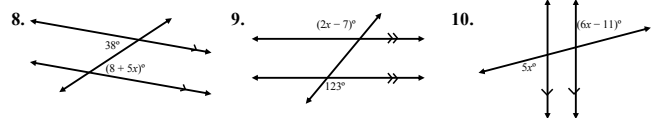
- Subtract $2x$ from each side.
- Add 58 to each side.
- Divide by 7 on each side.
- Write the given expression for each angle then substitute 9 for x .
 - $(2x + 5) = (2(9) + 5) = (18 + 5) = 23^\circ$
 - $(9x - 58) = (9(9) - 58) = (81 - 58) = 23^\circ$

L5 Practice Problems:

Name the special angle pair relationship.



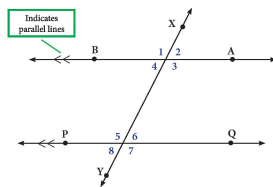
Name the special angle pair relationship. Solve for x .



END DAY 2

Day 3 L6: Corresponding and Same-Side Interior Angles

Vocabulary



Corresponding Angles: Two non-adjacent angles that are on the same side of a transversal with one angle is outside the two lines and the other angle is inside.

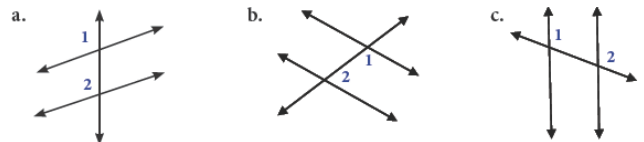
Same-Side Interior Angles: Two angles that are on the inside of two lines and are on the same side of the transversal.

$\angle 1$ & $\angle 5$ are corresponding angles.

$\angle 3$ & $\angle 6$ are same-side interior angles.

Example 1

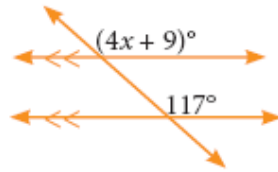
Name the special angle pair relationship between $\angle 1$ and $\angle 2$.



- corresponding angles
- same-side interior angles
- corresponding angles

Example 2

Write an equation and solve for x .



Corresponding angles have equal measures.

$$4x + 9 = 117$$

Subtract 9 from each side.

$$\begin{array}{r} -9 \quad -9 \\ 4x = 108 \end{array}$$

Divide by 4 on each side.

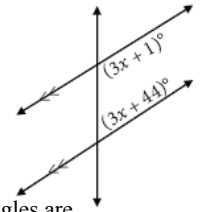
$$\begin{array}{r} 4 \quad 4 \\ x = 27 \end{array}$$

Check the solution by substituting 27 for x in the equation.

$$\begin{aligned} 4(27) + 9 &= 117 \\ 108 + 9 &= 117 \\ 117 &= 117 \checkmark \end{aligned}$$

Example 3

Write an equation and solve for x .
Then find the measure of each identified angle.



The lines are parallel so the same-side interior angles are supplementary.

$$(3x + 1) + (3x + 44) = 180$$

$$6x + 45 = 180$$

$$\begin{array}{r} -45 \quad -45 \\ 6x = 135 \end{array}$$

$$\begin{array}{r} 6 \quad 6 \\ x = 22.5 \end{array}$$

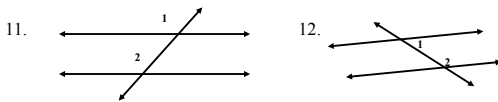
Find the measure of each angle by substituting 22.5 for x .

$$\begin{aligned} (3x + 1) &= (3(22.5) + 1) = (67.5 + 1) = 68.5^\circ \\ (3x + 44) &= (3(22.5) + 44) = (67.5 + 44) = 111.5^\circ \end{aligned}$$

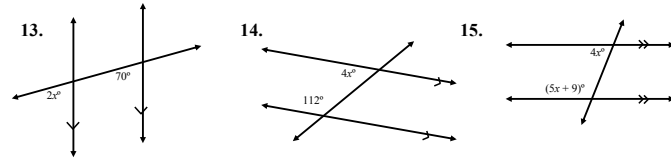
$$68.5 + 111.5 = 180 \checkmark$$

L6 Practice Problems:

Name the special angle pair relationship.



Name the special angle pair relationship. Solve for x .

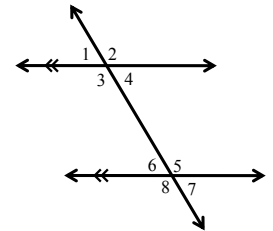


END DAY 3

Day 4

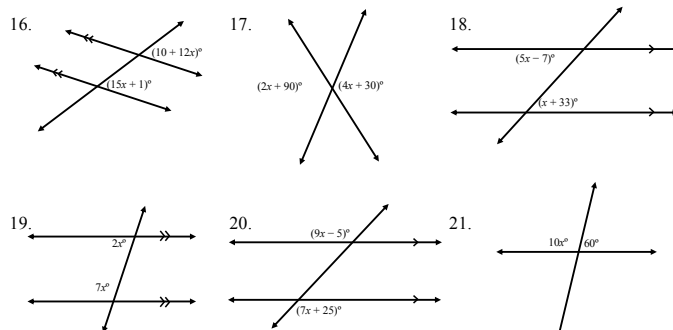
Angles of Two Parallel Lines Intersected by a Transversal

- ▶ Alternate exterior angles are congruent.
 - $\angle 1 \cong \angle 7$
 - $\angle 2 \cong \angle 8$
- ▶ Alternate interior angles are congruent.
 - $\angle 4 \cong \angle 6$
 - $\angle 3 \cong \angle 5$
- ▶ Corresponding angles are congruent.
 - $\angle 1 \cong \angle 6$
 - $\angle 2 \cong \angle 5$
 - $\angle 3 \cong \angle 8$
 - $\angle 4 \cong \angle 7$
- ▶ Same-Side interior angles are supplementary.
 - $m\angle 4 + m\angle 5 = 180^\circ$
 - $m\angle 3 + m\angle 6 = 180^\circ$



L4-6 Practice Problems:

Name the special angle pair relationship. Solve for x . Then find the measure of each identified angle.



END DAY 4

Practice Problems: ANSWER PAGE

Day 4:

- Corresponding; $x = 3$; 46°
- Vertical Angles; $x = 30$; 150°
- Alternate interior; $x = 10$; 43°
- Same-side interior; $x = 20$; 40° & 140°
- Alternate Exterior; $x = 15$; 130°
- Linear Pair; $x = 12$; 120°

Day 2:

- Alternate Exterior
- Alternate Interior
- Alternate Interior; $x = 6$
- Alternate Exterior; $x = 65$
- Alternate Exterior; $x = 11$

Day 3:

- Corresponding
- Same-side interior
- Corresponding, $x = 35$
- Same-side interior; $x = 17$
- Same-side interior; $x = 19$

Day 1:

- a) 74° b) 74° c) 106°
- Linear Pair; $x = 26$
- Vertical angles; $x = 12$
- Vertical angles; $x = 32$
- Linear pair; $x = 9$

MATH 7A: LAST SLIDE for this week!